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Recursion

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- There are two kinds of **repetitive technique**:
 - **Iterative**
 - **Recursive**
- **Iteration**
 - Iteration use **loops (for, while, or do)**.
 - Iteration often provide a **straightforward** and **efficient** way to implement a repetitive process.
 - Iterative solution is **complex**. **Discovering** or **verifying** such solution is **not simple task**. In these cases **recursion** is an elegant **alternative**.

Recursion

■ Recursion

- ❑ Recursion is an **important problem solving strategy**.
- ❑ Simple solution to difficult problems.
- ❑ **Programming technique** in which a **method call itself**.
- ❑ In **each call** the **argument** become **smaller** so the **problem** become **simpler**.
- ❑ **Recursive method** calls itself. When it calls itself, it does so to solve a **smaller problem**.

Decimal To Binary

Recursion

```
Class dectobin{
static int a = 2;
static int b =65;
public static void main(String [] args){
    performop(b,a);
}
public static void performop(int n, int s) {
if (n > 0 ) {
    performop (n/s, s);
    System.out.print(n % s);
}
}
}
```

Factorial

Recursion

$$N! = n*(n-1)*(n-2)*\dots*3*2*1$$

```
Public static int recursivefactorial(int n)
{
    if (n == 0) return 1;
    else return n*recursivefactorial(n-1);
}
```

Recursion

```
class factofN {
static int a;
static int b =7;
public static void main(String [] args){
    a= recursivefactorial(b);
    System.out.println(a);
}
public static int recursivefactorial(int n) {
    if (n == 0) return 1;
    else return n*recursivefactorial(n-1);
}
}
```

Counting the sum of $1+2+3+\dots+n$:

Recursion

```
class sumofnum {
static int a;
static int b =10;
public static void main(String [] args){
    a= sumof(b);
    System.out.println(a);
}
public static int sumof(int n) {
int sum;
if (n == 1)
sum = 1;
else
sum = sumof(n-1) + n;
return sum;
}
}
```

Write each digit vertically

Recursion

```
class vertnum {
static int n =3652;
public static void main(String [] args){
    writevertical(n);
}
public static void writevertical(int n) {
if (n<10)
System.out.println(n);
else
{
writevertical(n/10);
System.out.println(n % 10);
}
}
}
```


Fibonacci Sequence

Recursion

The fibonacci sequence is: 1,1,2,3,5,8,13,21

```
Long fib( int n) {
```

```
{
```

```
If (n<2) return n;
```

```
Return fib(n-1) + fib(n-2);
```

```
}
```

Recursion

```
public class FibonacciNumber {  
    public static void main (String [] args) {  
        int firstFibNum =3;  
        int secondFibNum =5;  
        int nth =6;  
        System.out.println("The Fibonacci number at position" + nth + "is:  
"  
        + rFibNum(firstFibNum, secondFibNum, nth));  
    }  
}
```

Recursion

```
public static int rFibNum(int a, int b, int n){
    if(n == 1)
        return a;
    else if(n==2)
        return b;
    else
        return rFibNum(a, b, n-1) + rFibNum(a, b, n-2);
}
```

Recursion

```
import java.io.*;
public class FibonacciNumber {
    static BufferedReader keyboard = new
        BufferedReader (new InputStreamReader (System.in));
    public static void main (String [] args) throws IOException {
        int firstFibNum;
        int secondFibNum;
        int nth;
        System.out.print("Enter the first Fibonacci Number: ");
        firstFibNum = Integer.parseInt(keyboard.readLine());
        System.out.println();

        System.out.print("Enter the second Fibonacci Number: ");
        secondFibNum = Integer.parseInt(keyboard.readLine());
        System.out.println();
```

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Recursion

```
System.out.print("Enter the position of the desired" + "Fibonacci number: ");
nth = Integer.parseInt(keyboard.readLine());
System.out.println();
System.out.println("The Fibonacci number at position" + nth + "is: "
    + rFibNum(firstFibNum, secondFibNum, nth));
}
```

Recursion

```
public static int rFibNum(int a, int b, int n){
    if(n == 1)
        return a;
    else if(n==2)
        return b;
    else
        return rFibNum(a, b, n-1) + rFibNum(a, b, n-2);
}
```

Fractals

Recursion

```
import java.applet.Applet;
import java.awt.*;
public class Fractal extends Applet {
    private Image display;
    private Graphics drawingArea;
```

Recursion

```
public void init() {
    int height = getSize().height;
    int width = getSize().width;
    display = createImage(width, height);
    drawingArea = display.getGraphics();
    randomFractal(0, height/2, width, height/2, drawingArea);
}

public void paint(Graphics g) {
    g.drawImage(display, 0, 0, null);
}
```


Recursion

```
public static void randomFractal  
(  
    int leftX,  
    int leftY,  
    int rightX,  
    int rightY,  
    Graphics drawingArea  
)
```

Recursion

```
{
    final int STOP =4;
    int midX, midY;
    int delta;
    if(( rightX - leftX) <= STOP)
        drawingArea.drawLine(leftX, leftY, rightX, rightY);
    else {
        midX = (leftX + rightX) /2;
        midY = (leftY + rightY) / 2;
        delta = (int) (( Math.random() - 0.5) * (rightX - leftX));
        midY += delta;
        randomFractal(leftX, leftY, midX, midY, drawingArea);
        randomFractal(midX, midY, rightX, rightY, drawingArea);
    }
}
```

The Towers of Hanoi

Recursion

- An **ancient puzzle**. There are **3 towers** and there are **7 disks** on tower A. The disks have **different diameter**.
- The **goal** is to **transfer** all the disks from tower **A** to tower **C** according to the following **rules**:
 - Carry **only one disk** at a time.
 - Never **put** a **big** disk on the **small** disk.
 - You can use **tower B** temporary.
- If the sub-tree has an **odd number** of disks, start by moving the topmost disk **directly** to the **tower** where you want the sub-tree to go.

Recursion

```
class towerapp {  
  
    static int ndisks =3;  
    public static void main (String[] args)  
    {  
        dotowers(ndisks, 'A', 'B', 'C');  
    }  
    public static void dotowers(int topn, char from, char inter, char to)  
    {  
        if(topn == 1)  
            System.out.println("Disk 1 from " + from + " to " + to);  
        else  
        {  
            dotowers(topn-1, from, to, inter);  
            System.out.println("Disk " + topn + "from " + from + "to " + to);  
            dotowers(topn-1, inter, from, to);  
        }  
    }  
}
```

Recursion

When tracing the code, the stack has the following status:

N	From	Inter	To	IP
1	A	B	C	
1	B	C	A	
2	B	A	C	2, 4
1	C	A	B	
1	A	B	C	
2	A	C	B	2, 4
3	A	B	C	2, 4

Traversing a Maze

Recursion

- Suppose the following **two facts** about a **maze**:
- Somewhere is a **panel** which contain the secret of the **universe**.
- You can keep this **panel** if you can **enter** the **maze**, **find** the **panel**, and **return** to the maze's **entrance**.
- The maze is built on a **rectangular grid**. At each **point** of the grid, there are **four directions** to **move**: **north**, **east**, **south**, or **west**. Some directions may be **blocked** by an impenetrable wall.
- You **accept** to enter the maze but only with the **help** of your **portable** computer and a **method** that we will write to **guide** you **into** the maze and **back out**.